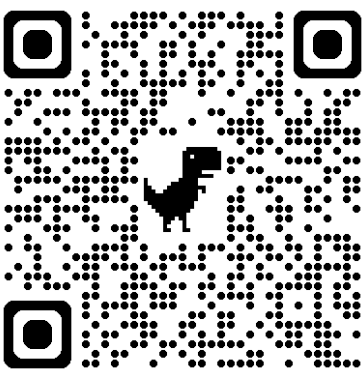


# Learning Identifiable Structures Helps Avoid Bias in DNN-based Supervised Causal Learning

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GitHub Repository:  
microsoft/reliableAI



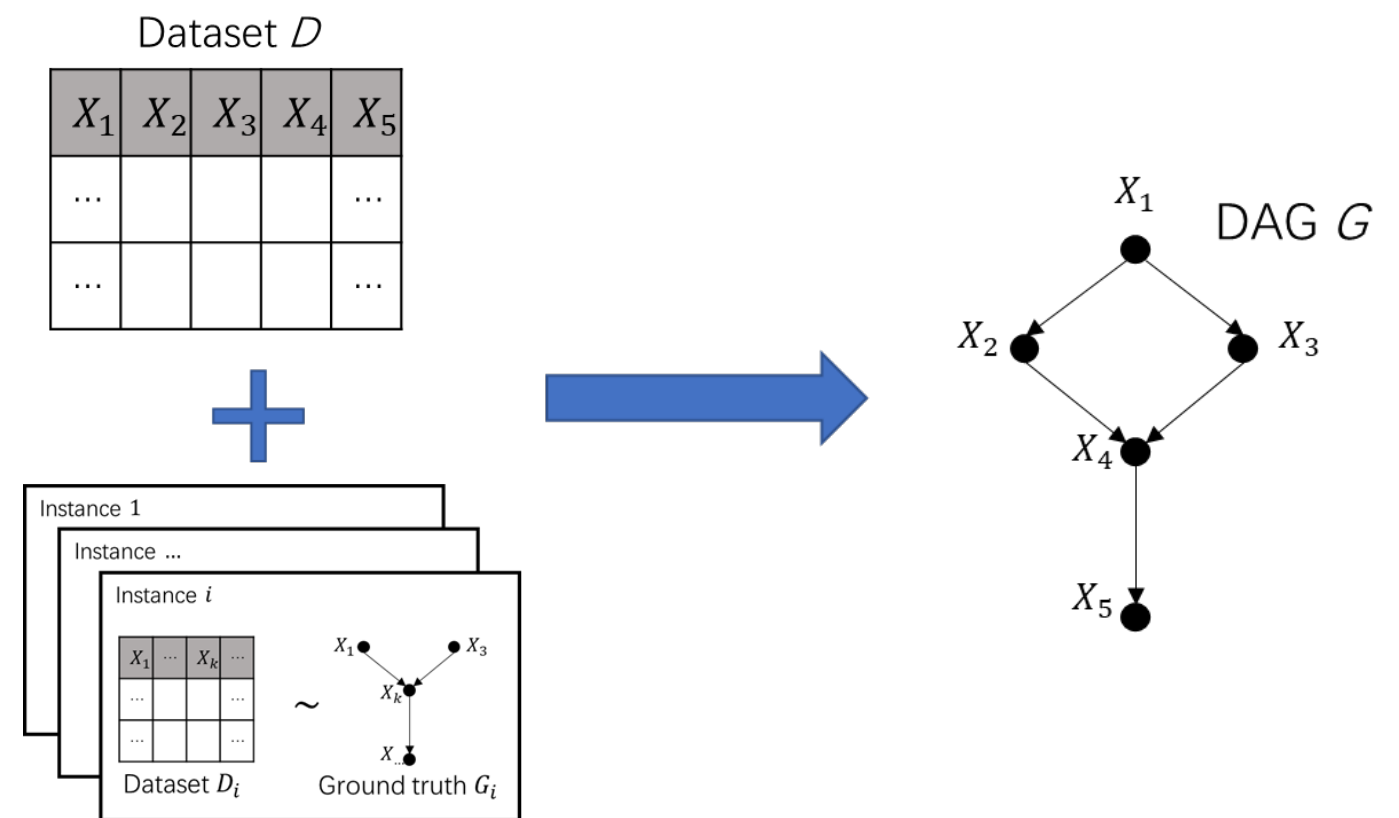
Microsoft

Sony Research



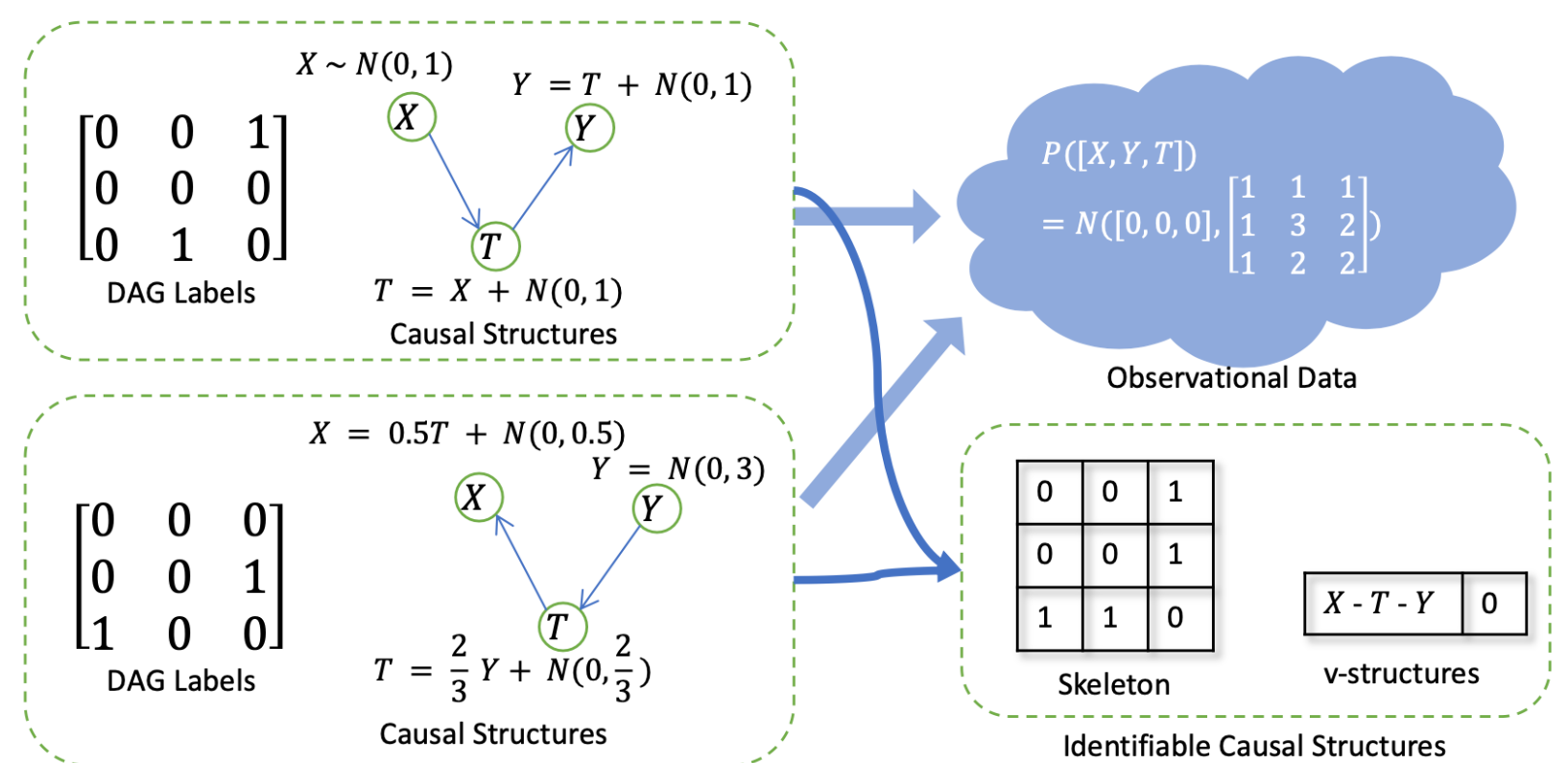
## Background

- Supervised Causal Learning (SCL): learning causal relations from observational data by accessing previously seen datasets associated with ground truth causal relations.
- Existing Node-Edge model: node-wise feature + independent Bernoulli edge distribution



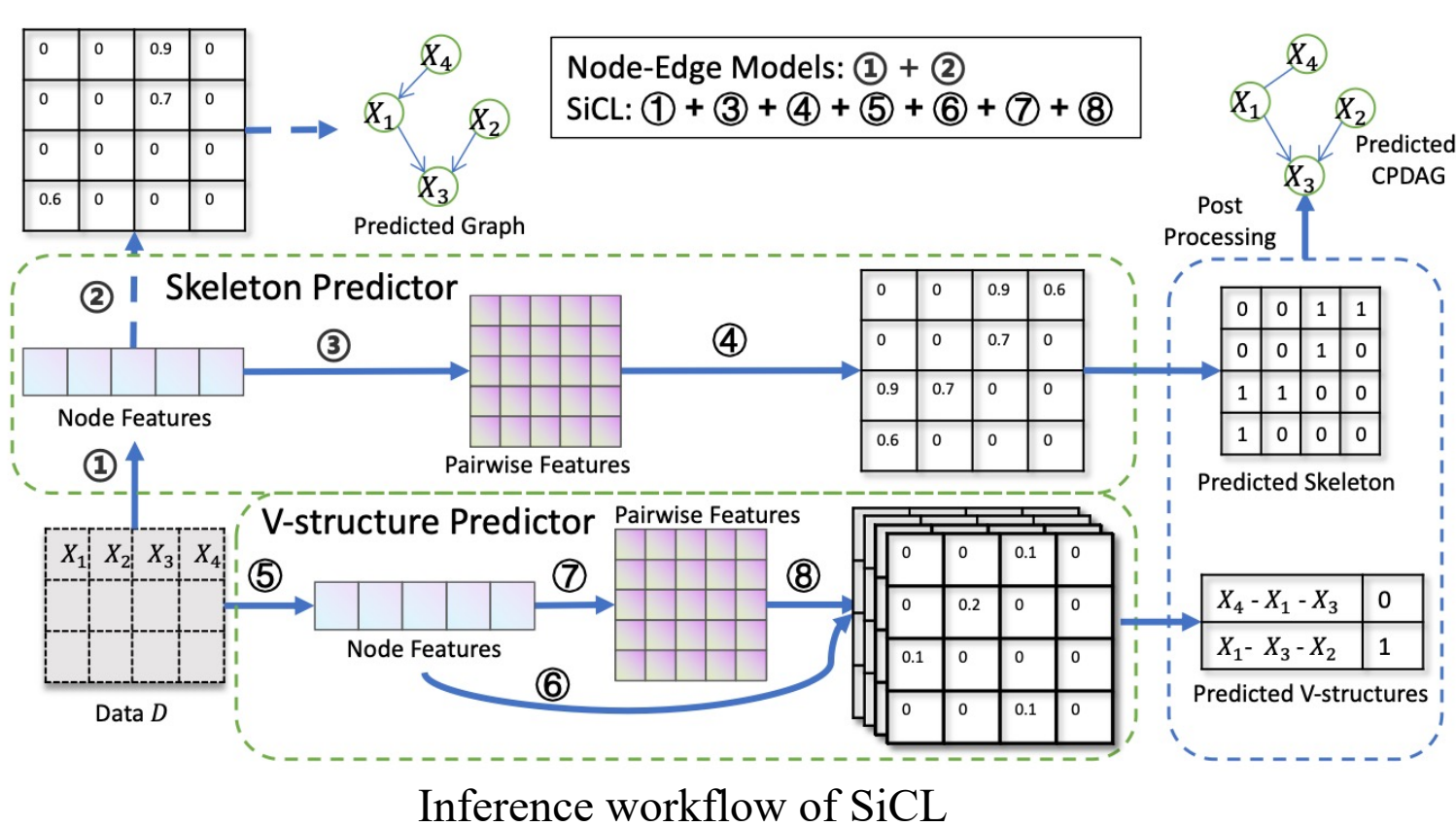
## Limitations of Node-Edge Model

- It has an unavoidable error rate under a presented three-variable demo.
- It has a higher error rate of  $\sim 0.2642$  under a more general scenario.
- It does not explicitly represent the essential features about node pairs.

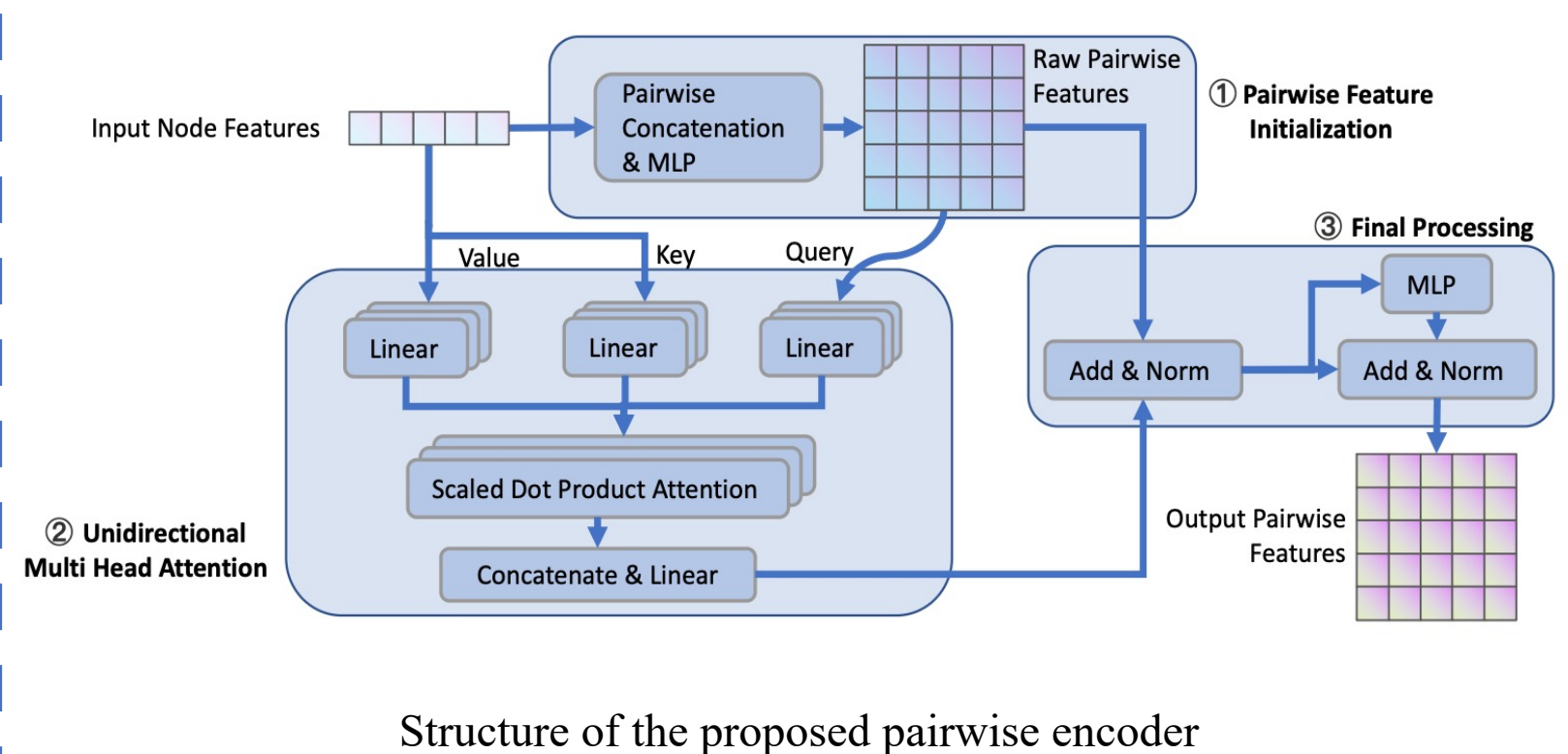


## Our SiCL Approach

- Learning *identifiable* causal structure: skeleton + v-structures with two separate DNNs.
- Utilizing a pairwise encoder to encode pairwise features explicitly.
- Theoretical guarantee: DNNs with our learning targets have a theoretical guarantee for correctness in asymptotic sense.



Inference workflow of SiCL



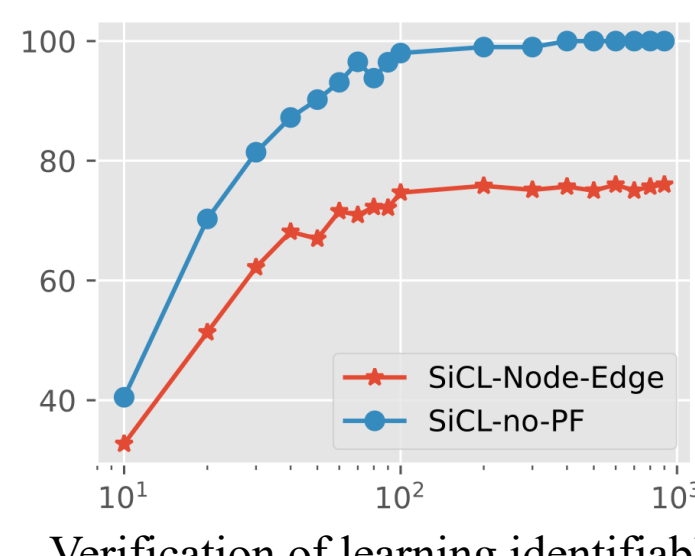
Structure of the proposed pairwise encoder

## Experimental Results

- SiCL outperforms various baselines on both synthetic datasets and real-world Sachs dataset.
- Ablation study confirms the effectiveness of learning identifiable structures and using pairwise representation.

A part of ablation study results

| Method         | WS-L-G      |             | SBM-L-G     |             |
|----------------|-------------|-------------|-------------|-------------|
|                | s-F1↑       | o-F1↑       | s-F1↑       | o-F1↑       |
| SiCL-Node-Edge | 39.9        | 35.8        | 84.3        | 81.6        |
| SiCL-no-PF     | 42.4        | 37.9        | 85.5        | 82.2        |
| SiCL           | <b>44.7</b> | <b>38.5</b> | <b>85.8</b> | <b>82.7</b> |



Verification of learning identifiable structures on a constructed dataset

Comparison on synthetic datasets

| Method   | WS-L-G      |             | SBM-L-G     |             | WS-RFF-G    |             | SBM-RFF-G   |             | ER-CPT-MC   |             |
|----------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|
|          | s-F1↑       | o-F1↑       | s-F1↑       | o-F1↑       | s-F1↑       | o-F1↑       | s-F1↑       | o-F1↑       | s-F1↑       | o-F1↑       |
| PC       | 30.4        | 16.0        | 58.8        | 35.9        | 36.1        | 16.1        | 57.5        | 34.2        | 82.2        | 40.6        |
| GES      | *           | *           | 70.8        | 55.0        | 41.7        | 23.6        | 56.5        | 38.0        | 82.1        | 42.4        |
| NOTEARS  | 33.3        | 31.5        | 80.1        | 77.8        | 37.7        | 33.4        | 55.6        | 48.5        | 16.7        | 0.6         |
| DAG-GNN  | 35.5        | 32.7        | 66.2        | 62.5        | 33.2        | 28.9        | 47.1        | 40.6        | 24.8        | 3.7         |
| GRAN-DAG | 16.6        | 11.7        | 22.6        | 14.4        | 4.7         | 1.1         | 17.4        | 3.8         | 40.8        | 7.3         |
| GOLEM    | 30.0        | 19.3        | 68.5        | 65.2        | 27.6        | 17.7        | 41.1        | 24.8        | 37.6        | 9.3         |
| AVICI    | 39.9        | 35.8        | 84.3        | 81.6        | 47.7        | 45.2        | 76.6        | 72.7        | 76.9        | 57.6        |
| SiCL     | <b>44.7</b> | <b>38.5</b> | <b>85.8</b> | <b>82.7</b> | <b>51.8</b> | <b>46.3</b> | <b>82.1</b> | <b>78.0</b> | <b>84.2</b> | <b>59.9</b> |

Comparison on Sachs dataset

| Method   | Skeleton Prediction |             | CPDAG Prediction |            |
|----------|---------------------|-------------|------------------|------------|
|          | s-F1↑               | s-Acc.↑     | SHD↓             | #v-struc.↓ |
| PC       | 68.6                | 80.0        | 19               | 12         |
| GES      | 70.6                | 81.8        | 19               | 8          |
| DAG-GNN  | 21.1                | 72.7        | 15               | <b>0</b>   |
| NOTEARS  | 11.1                | 70.9        | 16               | <b>0</b>   |
| GRAN-DAG | 45.5                | 78.2        | 12               | <b>0</b>   |
| GOLEM    | 36.4                | 74.5        | 14               | <b>0</b>   |
| AVICI    | 66.7                | 83.5        | 18               | 14         |
| SiCL     | <b>71.4</b>         | <b>86.8</b> | <b>6</b>         | <b>0</b>   |